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## Chapter 3: Quadratic Functions

## § 3.1: Properties of Quadratic Functions

## Parts of a Parabola



The graphs of quadratic functions have no $\qquad$ restrictions. Quadratic functions can be represented by $\qquad$ by $\qquad$ , or by $\qquad$ .

Quadratic Functions can be expressed in three different algebraic Forms:

| Factored Form | Vertex Form | Standard Form |
| :--- | :--- | :--- |

How can we determine whether a function is quadratic?

## Example 1: Linear or Quadratic?

a)

| $\mathbf{x}$ | $\mathbf{y}$ | FD | SD |
| :--- | :--- | :--- | :--- |
| -2 | 15 |  |  |
| -1 | 11 |  |  |
| 0 | 7 |  |  |
| 1 | 3 |  |  |
| 2 | -1 |  |  |

b)

| $\mathbf{x}$ | $\mathbf{y}$ | $\mathbf{F D}$ | $\mathbf{S D}$ |
| :--- | :--- | :--- | :--- |
| -2 | 7 |  |  |
| -1 | 4 |  |  |
| 0 | 3 |  |  |
| 1 | 4 |  |  |
| 2 | 7 |  |  |

In Class Assignment: p. $145 \# 1 \mathrm{bc}, 2,3$; Homework: p. $146 \# 4,5,7,8$

## § 3.2: Determining Maximum and Minimum Values of Quadratic Functions

The maximum or minimum value of a quadratic function is the $\qquad$ of the vertex.

If a $>0$ in standard form, factored form, or vertex form, then the parabola opens $\qquad$ .

The quadratic has a $\qquad$ value.

If $\mathrm{a}<0$ in standard form, factored form, or vertex form, then the parabola opens $\qquad$ .

The quadratic has a $\qquad$ value.

The vertex can be found from the standard form $f(x)=a x^{2}+b x+c$ algebraically:

- by $\qquad$ to put the quadratic in vertex form
- by expressing the quadratic in $\qquad$ , if possible, and averaging the zeros at $r$ and $s$ to locate the $\qquad$
- by $\qquad$ the common factor from $a x^{2}+b x$ to determine two points on the parabola that are symmetrically opposite each other, and averaging the $x$-coordinates to determine the $x$-coordinate of the vertex.
- by using a graphing calculator.


## Completing the Square:

$h(t)=5 t^{2}+40 t+100$

In Class Assignment: p. $153 \# 1,2,3$; Homework: p. $153 \# 4,5,7,9$

## § 3.3: Inverse of a Quadratic Function

The inverse of a quadratic function undoes what the original function has done. It is a
$\qquad$ relation that opens either to the $\qquad$ or to the $\qquad$ .

If the original quadratic opens up $(a>0)$, the inverse opens to the $\qquad$ .

If the original quadratic opens down ( $a<0$ ), the inverse opens to the $\qquad$ .

The equation of the inverse of a quadratic function can be found by $\qquad$ x and y
in the vertex form and solving for y .

In the equation of the inverse of a quadratic function, the $\qquad$ square root function
represents the $\qquad$ of the parabola, while the $\qquad$ square root
represents the $\qquad$ .

The inverse of a quadratic function can be a function if the $\qquad$ of the original function is

## Example: Determine the equation of the inverse

$$
f(x)=2(x+5)^{2}-3
$$

In Class Assignment: p. 160 \#1, 2, 3 ; Homework: p. 161 \#4, 5, 6, 7

## § 3.4: Operations With Radicals

Entire radicals can sometimes be simplified by expressing them as the $\qquad$ of two radicals, one of which contains a $\qquad$ . This results in a mixed radical.

- $\sqrt{a} \times \sqrt{b}=\sqrt{a b} \quad$ for $a \geq 0, b \geq 0$
- $c \sqrt{a} \times d \sqrt{b}=c d \sqrt{a b}$ for $a \geq 0, b \geq 0$

The only radicals that can be added or subtracted into a single term are $\qquad$ radicals.

An answer containing a radical is an $\qquad$ answer. An answer containing a decimal is an
$\qquad$ answer. A $\qquad$ radical is in simplest form when the smallest
possible number is written under the radical sign.

## Example 1: Simplifying radicals involving perfect-square factors

a) $\sqrt{72}$
b) $5 \sqrt{27}$

Example 2: Changing mixed radicals to entire radicals
a) $4 \sqrt{3}$
b) $-6 \sqrt{5}$

## Example 3: Multiplying Radicals

a) $\sqrt{3} \sqrt{11}$
b) $-2 \sqrt{6} \times 5 \sqrt{6}$
c) $(3-\sqrt{3})(3+\sqrt{6})$

In Class Assignment: p. 167 \#1, 2, 3; Homework: p. 168 \#4, 5, 6, 7, 13, 15

## § 3.5: Exploring Graphs of Rational Functions

All quadratic equations can be expressed in the form $a x^{2}+b x+c=0$ by algebraic techniques.

Quadratic equations can be solved by $\qquad$ the corresponding functions
$f(x)=a x^{2}+b x+c$ and locating the $\qquad$ , or $\qquad$ , either by hand or by technology. These zeros are the $\qquad$ or $\qquad$ of the equation $a x^{2}+b x+c=0$.

Quadratic equations can also be solved by $\qquad$ with the quadratic formula:


Depending on the problem and the degree of accuracy required, the solutions of a quadratic equation may be expressed exactly by using $\qquad$ or $\qquad$ numbers, or approximately with $\qquad$ .

## Example 1: Determine roots of equation by factoring

a) $x^{2}+5 x+4=0$
b) $2 x^{2}-7 x-4=0$

## Example 2: Use the quadratic formula to determine roots

b) $3 x^{2}+2 x-8=0$
b) $-2 x^{2}+3 x-6=0$

In Class Assignment: p. 177 \#1bc, 2ad, 4; Homework: p. 178 \#5, 6, 8, 17

## $\S 3.6$ - The Zeros of a Quadratic Function

A quadratic function can have $\qquad$ , $\qquad$ , or $\qquad$ zeros. You can determine the number of zeros either by $\qquad$ or by $\qquad$ the function. The number of zeros of a quadratic function can be determined by $\qquad$ , $\qquad$ and $\qquad$ . For a quadratic equation $a x^{2}+b x+c=0$ and
its corresponding function $f(x)=a x^{2}+b x+c$, use this table:

| Value of the Discriminant | Number of Zeros / Solutions |
| :---: | :---: |
| $b^{2}-4 a c>0$ | 2 |
| $b^{2}-4 a c=0$ | 1 |
| $b^{2}-4 a c<0$ | 0 |

The number of zeros can be determined by the location of the vertex relative to the $x$-axis, and the direction of opening:

- If a $>0$, and the vertex is above the x -axis, there are $\qquad$ zeros.
- If a $>0$, and the vertex is below the $x$-axis, there are $\qquad$ zeros.
- If a $<0$, and the vertex is above the x -axis, there are $\qquad$ zeros.
- If $\mathrm{a}<0$, and the vertex is below the x -axis, there are $\qquad$ zeros.
- If the vertex is on the x -axis, there is $\qquad$ zero.





## Example 1: State the number of zeros

a) $f(x)=3 x^{2}-5$
b) $f(x)=3(x+2)^{2}$
c) $f(x)=-4(x+3)^{2}-5$

Example 2: Calculate the value of $b^{2}-4 a c$ to determine the number of zeros
a) $f(x)=2 x^{2}-6 x-7$
b) $f(x)=9 x^{2}-14.4 x+5.76$

## § 3.7 - Families of a Quadratic Functions

If the value of $a$ is varied in a quadratic function expressed in a certain way, a family of parabolas similar to it will be created.

The algebraic model of a quadratic function can be determined algebraically.

- If the zeros are known, write in factored form with a unknown, substitute another known point, and solve for a.
- If the vertex is known, write in vertex form with a unknown, substitute a known point, and solve for $a$.


## Example 1: Determine the equation of parabola with x-intercepts

-4 and 3 , and that passes through $(2,7)$

## Example 2: Determine the equation of the parabola with vertex

$(-2,5)$ and that passes through $(4,-8)$

In Class Assignment: p. 192 \#1, 2, 3; Homework: p. 193 \#4bcd, 5bcd, 6, 7

